

Precalculus

TENTH EDITION

Michael Sullivan

ALWAYS LEARNING

0



To the Student

As you begin, you may feel anxious about the number of theorems, definitions, procedures, and equations. You may wonder if you can learn it all in time. Don't worry—your concerns are normal. This textbook was written with you in mind. If you attend class, work hard, and read and study this text, you will build the knowledge and skills you need to be successful. Here's how you can use the text to your benefit.

Read Carefully

When you get busy, it's easy to skip reading and go right to the problems. Don't ... the text has a large number of examples and clear explanations to help you break down the mathematics into easy-to-understand steps. Reading will provide you with a clearer understanding, beyond simple memorization. Read before class (not after) so you can ask questions about anything you didn't understand. You'll be amazed at how much more you'll get out of class if you do this.

Use the Features

I use many different methods in the classroom to communicate. Those methods, when incorporated into the text, are called "features." The features serve many purposes, from providing timely review of material you learned before (just when you need it) to providing organized review sessions to help you prepare for quizzes and tests. Take advantage of the features and you will master the material.

To make this easier, we've provided a brief guide to getting the most from this text. Refer to "Prepare for Class," "Practice," and "Review" on the following three pages. Spend fifteen minutes reviewing the guide and familiarizing yourself with the features by flipping to the page numbers provided. Then, as you read, use them. This is the best way to make the most of your text.

Please do not hesitate to contact us, through Pearson Education, with any questions, comments, or suggestions for improving this text. I look forward to hearing from you, and good luck with all of your studies.

Best Wishes! Michael Sullivan

Prepare for Class "Read the Book"

Feature	Description	Benefit	Page
Every Chapter Oper	ner begins with		
Chapter-Opening Topic & Project	Each chapter begins with a discussion of a topic of current interest and ends with a related project.	The Project lets you apply what you learned to solve a problem related to the topic.	282
M Internet-Based Projects	The projects allow for the integration of spreadsheet technology that you will need to be a productive member of the workforce.	The projects give you an opportunity to collaborate and use mathematics to deal with issues of current interest.	383
Every Section begin	ns with		
Learning Objectives	Each section begins with a list of objectives. Objectives also appear in the text where the objective is covered.	These focus your studying by emphasizing what's most important and where to find it.	303
Sections contain	•		
PREPARING FOR THIS SECTION	Most sections begin with a list of key concepts to review with page numbers.	Ever forget what you've learned? This feature highlights previously learned material to be used in this section. Review it, and you'll always be prepared to move forward.	
Now Work the 'Are You Prepared?' Problems	Problems that assess whether you have the prerequisite knowledge for the upcoming section.	Not sure you need the Preparing for This Section review? Work the 'Are You Prepared?' problems. If you get one wrong, you'll know exactly what you need to review and where to review it!	303, 314
Now Work PROBLEMS	These follow most examples and direct you to a related exercise.	We learn best by doing. You'll solidify your understanding of examples if you try a similar problem right away, to be sure you understand what you've just read.	310, 315
WARNING	Warnings are provided in the text.	These point out common mistakes and help you to avoid them.	336
Exploration and Seeing the Concept	These graphing utility activities foreshadow a concept or solidify a concept just presented.	You will obtain a deeper and more intuitive understanding of theorems and definitions.	298, 323
In Words	These provide alternative descriptions of select definitions and theorems.	Does math ever look foreign to you? This feature translates math into plain English.	320
Calculus	These appear next to information essential for the study of calculus.	Pay attention–if you spend extra time now, you'll do better later!	85, 287, 311
SHOWCASE EXAMPLES	These examples provide "how-to" instruction by offering a guided, step-by-step approach to solving a problem.	With each step presented on the left and the mathematics displayed on the right, you can immediately see how each step is employed.	214
Model It! Examples and Problems	These examples and problems require you to build a mathematical model from either a verbal description or data. The homework Model It! problems are marked by purple headings.	It is rare for a problem to come in the form "Solve the following equation." Rather, the equation must be developed based on an explanation of the problem. These problems require you to develop models that will allow you to describe the problem mathematically and suggest a solution to the problem.	327, 355

Practice "Work the Problems"

Feature	Description	Benefit	Page
'Are You Prepared?' Problems	These assess your retention of the prerequisite material you'll need. Answers are given at the end of the section exercises. This feature is related to the Preparing for This Section feature.	Do you always remember what you've learned? Working these problems is the best way to find out. If you get one wrong, you'll know exactly what you need to review and where to review it!	314, 328
Concepts and Vocabulary	These short-answer questions, mainly Fill-in-the-Blank, Multiple-Choice and True/False items, assess your understanding of key definitions and concepts in the current section.	It is difficult to learn math without knowing the language of mathematics. These problems test your understanding of the formulas and vocabulary.	314
Skill Building	Correlated with section examples, these problems provide straightforward practice.	It's important to dig in and develop your skills. These problems provide you with ample opportunity to do so.	314–316
Mixed Practice	These problems offer comprehensive assessment of the skills learned in the section by asking problems that relate to more than one concept or objective. These problems may also require you to utilize skills learned in previous sections.	Learning mathematics is a building process. Many concepts are interrelated. These problems help you see how mathematics builds on itself and also see how the concepts tie together.	316–317
Applications and Extensions	These problems allow you to apply your skills to real-world problems. They also allow you to extend concepts learned in the section.	You will see that the material learned within the section has many uses in everyday life.	317-319
Explaining Concepts: Discussion and Writing	"Discussion and Writing" problems are colored red. They support class discussion, verbalization of mathematical ideas, and writing and research projects.	To verbalize an idea, or to describe it clearly in writing, shows real understanding. These problems nurture that understanding. Many are challenging, but you'll get out what you put in.	
NEW! Retain Your Knowledge	These problems allow you to practice content learned earlier in the course.	Remembering how to solve all the different kinds of problems that you encounter throughout the course is difficult. This practice helps you remember.	319
Now Work Problems	Many examples refer you to a related homework problem. These related problems are marked by a pencil and orange numbers.	If you get stuck while working problems, look for the closest Now Work problem, and refer to the related example to see if it helps.	312, 315, 316
Review Exercises	Every chapter concludes with a comprehensive list of exercises to pratice. Use the list of objectives to determine the objective and examples that correspond to the problems.	Work these problems to ensure that you understand all the skills and concepts of the chapter. Think of it as a comprehensive review of the chapter.	379–381

Review "Study for Quizzes and Tests"

Feature	Description	Benefit	Page
The Chapter Revie	w at the end of each chapter contains		
Things to Know	A detailed list of important theorems, formulas, and definitions from the chapter.	Review these and you'll know the most important material in the chapter!	377–378
You Should Be Able to	Contains a complete list of objectives by section, examples that illustrate the objective, and practice exercises that test your understanding of the objective.	Do the recommended exercises and you'll have mastered the key material. If you get something wrong, go back and work through the example listed and try again.	378–379
Review Exercises	These provide comprehensive review and practice of key skills, matched to the Learning Objectives for each section.	Practice makes perfect. These problems combine exercises from all sections, giving you a comprehensive review in one place.	379–381
Chapter Test	About 15–20 problems that can be taken as a Chapter Test. Be sure to take the Chapter Test under test conditions—no notes!	Be prepared. Take the sample practice test under test conditions. This will get you ready for your instructor's test. If you get a problem wrong, you can watch the Chapter Test Prep Video.	382
Cumulative Review	These problem sets appear at the end of each chapter, beginning with Chapter 2. They combine problems from previous chapters, providing an ongoing cumulative review. When you use them in conjunction with the Retain Your Knowledge problems, you will be ready for the final exam.	These problem sets are really important. Completing them will ensure that you are not forgetting anything as you go. This will go a long way toward keeping you primed for the final exam.	382–383
Chapter Projects	The Chapter Projects apply to what you've learned in the chapter. Additional projects are available on the Instructor's Resource Center (IRC).	The Chapter Projects give you an opportunity to apply what you've learned in the chapter to the opening topic. If your instructor allows, these make excellent opportunities to work in a group, which is often the best way of learning math.	383–384
M Internet-Based Projects	In selected chapters, a Web-based project is given.	These projects give you an opportunity to collaborate and use mathematics to deal with issues of current interest by using the Internet to research and collect data.	383

Achieve Your Potential

The author, Michael Sullivan, has developed specific content in MyMathLab[®] to ensure you have many resources to help you achieve success in mathematics - and beyond! The MyMathLab features described here will help you:

- **Review** math skills and concepts you may have forgotten
- **Retain** new concepts as you move through your math course

Study Plan

• Develop skills that will help with your transition to college

Adaptive Study Plan

The Study Plan will help you study more efficiently and effectively.

Your performance and activity are assessed continually in real time, providing a personalized experience based on your individual needs.



Skills for Success

The Skills for Success Modules support your continued success in college. These modules provide tutorials and guidance on a variety of topics, including transitioning to college, online learning, time management, and more.

Additional content is provided to help with the development of professional skills such as resume writing and interview preparation.



Stu	dy Pl	lan				
íou	nave e	arned 0 of 687 mastery points (MP).			View progress	
rac	ice the	se objectives and then take a Quiz Me to prove mastery and earn more points.				
w	hat t	o work on next				
	GR.1	Real Number System				
	*	Identify types of numbers.	Practice	Quiz Me	0 of 1 MP	
•	*	More Objectives to practice and master			Yiew all chapters	
	GR.1	Real Number System				
	*	Graph numbers on a number line.	Practice	Quiz Me	0 of 1 MP	
	*	Find absolute values.	Practice	Quiz Me	0 of 1 MP	
	*	Calculate with real numbers.	Practice	Quiz Me	0 of 1 MP	
	*	Use the properties of real numbers.	Practice	Quiz Me	0 of 1 MP	
					MyMath	

Getting Ready

Are you frustrated when you know you learned a math concept in the past, but you can't quite remember the skill when it's time to use it? Don't worry!

The author has included Getting Ready material so you can brush up on forgotten material efficiently by taking a

nodify 🗘 🔄	S Homewo	ork
Course Home	() Due	Assignment
Homework	12/27/13 11:59pm	💠 Chapter 1 Fost-Test
Quizzes & Tests	01/28/14 11:59pm	Getting Ready for Chapter 2 Quiz
Study Plan	01/28/14 11:59pm	Getting Ready for Chapter 2 Homework
Gradebook	01/28/14	Chapter 2 Fre-Test
▼ Chapter Contents	11:59pm 01/28/14	B Section 2.1 Homework
Student Solutions Manual	11:59pm 01/28/14 11:59pm	0 Section 2.2 Homework
Online Only: Getting Ready for College	01/28/14 11:59pm	Bection 2.3 Homework
Algebra	01/28/14 11:59pm	B Section 2.4 Homework
Chapter 1	01/28/14 11:59pm	B Section 2.5 Homework
Chapter 2	01/28/14 11:59pm	Chapter 2 Review Quiz
Getting Ready for Chapter 2	01/28/14 F 11:59pm	(1) Chapter 2 Review Homework
Section 2.1	01/28/14 11:59pm	Chapter 2 Fost-Test

quick skill review quiz to pinpoint the areas where you need help.

Then, a personalized homework assignment provides additional practice on those forgotten concepts, right when you need it.



Retain Your Knowledge

As you work through your math course, these MyMathLab[®] exercises support ongoing review to help you maintain essential skills.

The ability to recall important math concepts as you continually acquire new mathematical skills will help you be successful in this math course and in your future math courses.

Precalculus

Tenth Edition Global Edition

Michael Sullivan

Chicago State University



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To the Memory of My Mother and Father

Three Distinct Series

Students have different goals, learning styles, and levels of preparation. Instructors have different teaching philosophies, styles, and techniques. Rather than write one series to fit all, the Sullivans have written three distinct series. All share the same goal—to develop a high level of mathematical understanding and an appreciation for the way mathematics can describe the world around us. The manner of reaching that goal, however, differs from series to series.

Contemporary Series, Tenth Edition

The Contemporary Series is the most traditional in approach yet modern in its treatment of precalculus mathematics. Graphing utility coverage is optional and can be included or excluded at the discretion of the instructor: *College Algebra, Algebra & Trigonometry, Trigonometry: A Unit Circle Approach, Precalculus.*

Enhanced with Graphing Utilities Series, Sixth Edition

This series provides a thorough integration of graphing utilities into topics, allowing students to explore mathematical concepts and encounter ideas usually studied in later courses. Using technology, the approach to solving certain problems differs from the Contemporary Series, while the emphasis on understanding concepts and building strong skills does not: *College Algebra, Algebra & Trigonometry, Precalculus*.

Concepts through Functions Series, Third Edition

This series differs from the others, utilizing a functions approach that serves as the organizing principle tying concepts together. Functions are introduced early in various formats. This approach supports the Rule of Four, which states that functions are represented symbolically, numerically, graphically, and verbally. Each chapter introduces a new type of function and then develops all concepts pertaining to that particular function. The solutions of equations and inequalities, instead of being developed as stand-alone topics, are developed in the context of the underlying functions. Graphing utility coverage is optional and can be included or excluded at the discretion of the instructor: *College Algebra; Precalculus, with a Unit Circle Approach to Trigonometry; Precalculus, with a Right Triangle Approach to Trigonometry.*

The Contemporary Series

College Algebra, Tenth Edition

This text provides a contemporary approach to college algebra, with three chapters of review material preceding the chapters on functions. Graphing calculator usage is provided, but is optional. After completing this book, a student will be adequately prepared for trigonometry, finite mathematics, and business calculus.

Algebra & Trigonometry, Tenth Edition

This text contains all the material in *College Algebra*, but also develops the trigonometric functions using a right triangle approach and showing how it relates to the unit circle approach. Graphing techniques are emphasized, including a thorough discussion of polar coordinates, parametric equations, and conics using polar coordinates. Graphing calculator usage is provided, but is optional. After completing this book, a student will be adequately prepared for finite mathematics, business calculus, and engineering calculus.

Precalculus, Tenth Edition

This text contains one review chapter before covering the traditional precalculus topic of functions and their graphs, polynomial and rational functions, and exponential and logarithmic functions. The trigonometric functions are introduced using a unit circle approach and showing how it relates to the right triangle approach. Graphing techniques are emphasized, including a thorough discussion of polar coordinates, parametric equations, and conics using polar coordinates. Graphing calculator usage is provided, but is optional. The final chapter provides an introduction to calculus, with a discussion of the limit, the derivative, and the integral of a function. After completing this book, a student will be adequately prepared for finite mathematics, business calculus, and engineering calculus.

Trigonometry: a Unit Circle Approach, Tenth Edition

This text, designed for stand-alone courses in trigonometry, develops the trigonometric functions using a unit circle approach and showing how it relates to the right triangle approach. Graphing techniques are emphasized, including a thorough discussion of polar coordinates, parametric equations, and conics using polar coordinates. Graphing calculator usage is provided, but is optional. After completing this book, a student will be adequately prepared for finite mathematics, business calculus, and engineering calculus.

Preface to the Instructor

s a professor of mathematics at an urban public university for 35 years, I understand the varied needs of precalculus students. Students range from being underprepared, with little mathematical background and a fear of mathematics, to being highly prepared and motivated. For some, this is their final course in mathematics. For others, it is preparation for future mathematics courses. I have written this text with both groups in mind.

A tremendous benefit of authoring a successful series is the broad-based feedback I receive from teachers and students who have used previous editions. I am sincerely grateful for their support. Virtually every change to this edition is the result of their thoughtful comments and suggestions. I hope that I have been able to take their ideas and, building upon a successful foundation of the ninth edition, make this series an even better learning and teaching tool for students and teachers.

Features in the Tenth Edition

A descriptive list of the many special features of *Precalculus* can be found on the endpapers in the front of this text.

This list places the features in their proper context, as building blocks of an overall learning system that has been carefully crafted over the years to help students get the most out of the time they put into studying. Please take the time to review this and to discuss it with your students at the beginning of your course. My experience has been that when students utilize these features, they are more successful in the course.

New to the Tenth Edition

- **Retain Your Knowledge** This new category of problems in the exercise set are based on the article "To Retain New Learning, Do the Math" published in the *Edurati Review*. In this article, Kevin Washburn suggests that "the more students are required to recall new content or skills, the better their memory will be." It is frustrating when students cannot recall skills learned earlier in the course. To alleviate this recall problem, we have created "Retain Your Knowledge" problems. These are problems considered to be "final exam material" that students can use to maintain their skills. Answers to all these problems appear in the back of the book, and all are programmed in MyMathLab.
- Guided Lecture Notes Ideal for online, emporium/ redesign courses, inverted classrooms, or traditional lecture classrooms. These lecture notes help students take thorough, organized, and understandable notes as they watch the Author in Action videos. They ask students to complete definitions, procedures, and examples based on the content of the videos and text. In addition, experience suggests that students learn by doing and understanding the why/how of the concept or

property. Therefore, many sections will have an exploration activity to motivate student learning. These explorations introduce the topic and/or connect it to either a real-world application or a previous section. For example, when the vertical-line test is discussed in Section 2.2, after the theorem statement, the notes ask the students to explain why the vertical-line test works by using the definition of a function. This challenge helps students process the information at a higher level of understanding.

- **Illustrations** Many of the figures now have captions to help connect the illustrations to the explanations in the body of the text.
- **TI Screen Shots** In this edition we have replaced all the screen shots from the ninth edition with screen shots using TI-84Plus C. These updated screen shots help students visualize concepts clearly and help make stronger connections between equations, data, and graphs in full color.
- Chapter Projects, which apply the concepts of each chapter to a real-world situation, have been enhanced to give students an up-to-the-minute experience. Many projects are new and Internet-based, requiring the student to research information online in order to solve problems.
- **Exercise Sets** All the exercises in the text have been reviewed and analyzed for this edition, some have been removed, and new ones have been added. All time-sensitive problems have been updated to the most recent information available. The problem sets remain classified according to purpose.

The 'Are You Prepared?' problems have been improved to better serve their purpose as a just-in-time review of concepts that the student will need to apply in the upcoming section.

The *Concepts and Vocabulary* problems have been expanded and now include multiple-choice exercises. Together with the fill-in-the-blank and True/False problems, these exercises have been written to serve as reading quizzes.

Skill Building problems develop the student's computational skills with a large selection of exercises that are directly related to the objectives of the section. *Mixed Practice* problems offer a comprehensive assessment of skills that relate to more than one objective. Often these require skills learned earlier in the course.

Applications and Extensions problems have been updated. Further, many new application-type exercises have been added, especially ones involving information and data drawn from sources the student will recognize, to improve relevance and timeliness.

The *Explaining Concepts: Discussion and Writing* exercises have been improved and expanded to provide more opportunity for classroom discussion and group projects.

New to this edition, *Retain Your Knowledge* exercises consist of a collection of four problems in each exercise set that are based on material learned earlier in the course. They serve to keep information that has already been learned "fresh" in the mind of the student. Answers to all these problems appear in the book.

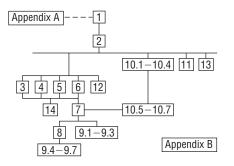
The *Review Exercises* in the Chapter Review have been streamlined, but they remain tied to the clearly expressed objectives of the chapter. Answers to all these problems appear in the book.

Content Changes in the Tenth Edition

- **Section 2.1** The objective Find the Difference Quotient of a Function has been added.
- **Section 4.1** The subsection Behavior of the Graph of a Polynomial Function Near a Zero has been removed.
- Section 4.3 A subsection has been added that discusses the role of multiplicity of the zeros of the denominator of a rational function as it relates to the graph near a vertical asymptote.
- Section 4.5 The objective Use Descartes' Rule of Signs has been included.
- Section 4.5 The theorem Bounds on the Zeros of a Polynomial Function is now based on the traditional method of using synthetic division.

Using the Tenth Edition Effectively with Your Syllabus

To meet the varied needs of diverse syllabi, this text contains more content than is likely to be covered in a *Precalculus* course. As the chart illustrates, this text has been organized with flexibility of use in mind. Within a given chapter, certain sections are optional (see the details that follow the figure below) and can be omitted without loss of continuity.



Appendix A Review

This chapter consists of review material. It may be used as the first part of the course or later as a just-in-time review when the content is required. Specific references to this chapter occur throughout the book to assist in the review process.

Chapter 1 Graphs

This chapter lays the foundation for functions.

Chapter 2 Functions and Their Graphs Perhaps the most important chapter. Section 2.6 is optional.

Chapter 3 Linear and Quadratic Functions

Topic selection depends on your syllabus. Sections 3.2 and 3.4 may be omitted without loss of continuity.

Chapter 4 Polynomial and Rational Functions Topic selection depends on your syllabus.

Chapter 5 Exponential and Logarithmic Functions

Sections 5.1–5.6 follow in sequence. Sections 5.7, 5.8, and 5.9 are optional.

Chapter 6 Trigonometric Functions

Section 6.6 may be omitted in a brief course.

Chapter 7 Analytic Trigonometry

Sections 7.7 may be omitted in a brief course.

Chapter 8 Applications of Trigonometric Functions

Sections 8.4 and 8.5 may be omitted in a brief course.

Chapter 9 Polar Coordinates; Vectors

Sections 9.1–9.3 and Sections 9.4–9.7 are independent and may be covered separately.

Chapter 10 Analytic Geometry

Sections 10.1–10.4 follow in sequence. Sections 10.5, 10.6, and 10.7 are independent of each other, but each requires Sections 10.1–10.4.

Chapter 11 Systems of Equations and Inequalities

Sections 11.2–11.7 may be covered in any order, but each requires Section 11.1. Section 11.8 requires Section 11.7.

Chapter 12 Sequences; Induction; The Binomial Theorem

There are three independent parts: Sections 12.1–12.3; Section 12.4; and Section 12.5.

Chapter 13 Counting and Probability

The sections follow in sequence.

Chapter 14 A Preview of Calculus: The Limit, Derivative, and Integral of a Function

If time permits, coverage of this chapter will give your students a beneficial head start in calculus.

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James Africh, College of DuPage

Carolyn Bernath, Tallahassee Community College

Rebecca Berthiaume, Edison State College William H. Beyer, University of Akron Annette Blackwelder, Florida State University Richelle Blair, Lakeland Community College Kevin Bodden, Lewis and Clark College Jeffrey Boerner, University of Wisconsin-Stout Barry Booten, Florida Atlantic University Larry Bouldin, Roane State Community College

Bob Bradshaw, Ohlone College Trudy Bratten, Grossmont College Tim Bremer, Broome Community College Tim Britt, Jackson State Community College Michael Brook, University of Delaware Joanne Brunner, Joliet Junior College Warren Burch, Brevard Community College Mary Butler, Lincoln Public Schools Melanie Butler, West Virginia University Jim Butterbach, Joliet Junior College William J. Cable, University of

Wisconsin-Stevens Point Lois Calamia, Brookdale Community College Jim Campbell, Lincoln Public Schools Roger Carlsen, Moraine Valley Community College

Elena Catoiu, Joliet Junior College Mathews Chakkanakuzhi, Palomar College Tim Chappell, Penn Valley Community College John Collado, South Suburban College Alicia Collins, Mesa Community College Nelson Collins, Joliet Junior College Rebecca Connell, Troy University Jim Cooper, Joliet Junior College Denise Corbett, East Carolina University

Carlos C. Corona, San Antonio College Theodore C. Coskey, South Seattle Community College Donna Costello, Plano Senior High School Paul Crittenden, University of Nebraska at Lincoln Faye Dang, Joliet Junior College John Davenport, East Texas State University Antonio David, Del Mar College Stephanie Deacon, Liberty University Duane E. Deal, Ball State University Jerry DeGroot, Purdue North Central Timothy Deis, University of Wisconsin-Platteville Joanna DelMonaco, Middlesex Community College Vivian Dennis, Eastfield College Deborah Dillon, R. L. Turner High School Guesna Dohrman, Tallahassee Community College Cheryl Doolittle, Iowa State University Karen R. Dougan, University of Florida Jerrett Dumouchel, Florida Community College at Jacksonville Louise Dyson, Clark College Paul D. East, Lexington Community College Don Edmondson, University of Texas-Austin Erica Egizio, Joliet Junior College Jason Eltrevoog, Joliet Junior College Christopher Ennis, University of Minnesota Kathy Eppler, Salt Lake Community College Ralph Esparza, Jr., Richland College Garret J. Etgen, University of Houston Scott Fallstrom, Shoreline Community College Pete Falzone, Pensacola Junior College Arash Farahmand, Skyline College W.A. Ferguson, University of Illinois-Urbana/ Champaign Iris B. Fetta, Clemson University Mason Flake, student at Edison Community College Timothy W. Flood, Pittsburg State University Robert Frank, Westmoreland County Community College Merle Friel, Humboldt State University Richard A. Fritz, Moraine Valley Community College Dewey Furness, Ricks College Mary Jule Gabiou, North Idaho College Randy Gallaher, Lewis and Clark College Tina Garn, University of Arizona Dawit Getachew, Chicago State University Wayne Gibson, Rancho Santiago College

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Donna Katula, Joliet Junior College

Charlotte Smedberg, University of Tampa

Cindy Soderstrom, Salt Lake Community

Karen Spike, University of North Carolina

Katrina Staley, North Carolina Agricultural

Robin Steinberg, Pima Community College

Neil Stephens, Hinsdale South High School

Sonva Stephens, Florida A&M University

Matthew TenHuisen, University of North

Christopher Terry, Augusta State University

Martha K. Tietze, Shawnee Mission Northwest

Patrick Stevens, Joliet Junior College

Diane Tesar, South Suburban College

Tommy Thompson, Brookhaven College

Richard J. Tondra, Iowa State University

Florentina Tone, University of West Florida

Marilyn Toscano, University of Wisconsin,

Marvel Townsend, University of Florida

Jim Trudnowski, Carroll College

College-Leesville

Robert Tuskey, Joliet Junior College

Suzanne Topp, Salt Lake Community College

Mihaela Vajiac, Chapman University-Orange

Jorge Viola-Prioli, Florida Atlantic University

Donna Wandke, Naperville North High School

Jennifer Walsh, Daytona Beach Community

Julia Varbalow, Thomas Nelson Community

Richard G. Vinson, University of South

Mary Voxman, University of Idaho

Timothy L.Warkentin, Cloud County

Melissa J. Watts, Virginia State University

Hayat Weiss, Middlesex Community College

Community College

Kathryn Wetzel, Amarillo College

John Sumner, University of Tampa

Carolina, Wilmington

High School

Superior

Alabama

College

and Technical State University

Becky Stamper, Western Kentucky

Judy Staver, Florida Community

Gayle Smith, Loyola Blakefield

Leslie Soltis, Mercyhurst College

John Spellman, Southwest Texas State

Rajalakshmi Sriram, Okaloosa-Walton Community College

College

University

University

College-South

Lori Smellegar, Manatee Community College

Arthur Kaufman, College of Staten Island Thomas Kearns, North Kentucky University Jack Keating, Massasoit Community College Shelia Kellenbarger, Lincoln Public Schools Rachael Kenney, North Carolina State University

John B. Klassen, North Idaho College Debra Kopcso, Louisiana State University Lynne Kowski, Raritan Valley Community College

Yelena Kravchuk, University of Alabama at Birmingham

Ray S. Kuan, Skyline College

Keith Kuchar, Manatee Community College Tor Kwembe, Chicago State University Linda J. Kyle, Tarrant Country Jr. College

H.E. Lacey, Texas A & M University Harriet Lamm, Coastal Bend College

James Lapp, Fort Lewis College

Matt Larson, Lincoln Public Schools

- Christopher Lattin, Oakton Community College Julia Ledet, Lousiana State University
- Adele LeGere, Oakton Community College
- Kevin Leith, University of Houston

JoAnn Lewin, Edison College

Jeff Lewis, Johnson County Community College

Janice C. Lyon, Tallahassee Community College

Jean McArthur, Joliet Junior College

Virginia McCarthy, Iowa State University

Karla McCavit, Albion College

Michael McClendon, University of Central Oklahoma

Tom McCollow, DeVry Institute of Technology Marilyn McCollum, North Carolina State University

Jill McGowan, Howard University Will McGowant, Howard University Angela McNulty, Joliet Junior College Laurence Maher, North Texas State University Jay A. Malmstrom, Oklahoma City Community

College Rebecca Mann, Apollo High School

Lynn Marecek, Santa Ana College Sherry Martina, Naperville North High School

Alec Matheson, Lamar University

Nancy Matthews, University of Oklahoma James Maxwell, Oklahoma State

University-Stillwater

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Baltimore County Val Mohanakumar, Hillsborough Community College

Thomas Monaghan, Naperville North High School

Miguel Montanez, Miami Dade College, Wolfson Campus

Maria Montoya, Our Lady of the Lake University

Susan Moosai, Florida Atlantic University

Craig Morse, Naperville North High School Samad Mortabit, Metropolitan State University Pat Mower, Washburn University Tammy Muhs, University of Central Florida A. Muhundan, Manatee Community College Jane Murphy, Middlesex Community College Richard Nadel, Florida International University Bill Naegele, South Suburban College Gabriel Nagy, Kansas State University Karla Neal, Lousiana State University Lawrence E. Newman, Holyoke Community College

Dwight Newsome, Pasco-Hernando Community College

Denise Nunley, Maricopa Community Colleges James Nymann, University of Texas-El Paso Mark Omodt, Anoka-Ramsey Community

College Seth F. Oppenheimer, Mississippi State

University

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- Linda Padilla, Joliet Junior College
- Sanja Pantic, University of Illinois at Chicago
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- Philip Pina, Florida Atlantic University

Charlotte Pisors, Baylor University

Michael Prophet, University of Northern Iowa

Laura Pyzdrowski, West Virginia University

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Neal C. Raber, University of Akron

Thomas Radin, San Joaquin Delta College Aibeng Serene Radulovic, Florida Atlantic University

Ken A. Rager, Metropolitan State College

Kenneth D. Reeves, San Antonio College

Elsi Reinhardt, Truckee Meadows Community College

Jose Remesar, Miami Dade College, Wolfson Campus

Jane Ringwald, Iowa State University

Douglas F. Robertson, University of Minnesota, MPLS

Stephen Rodi, Austin Community College William Rogge, Lincoln Northeast High School

Howard L. Rolf, Baylor University

Mike Rosenthal, Florida International

University

Phoebe Rouse, Lousiana State University

Edward Rozema, University of Tennessee at Chattanooga

Dennis C. Runde, Manatee Community College

Alan Saleski, Loyola University of Chicago

Susan Sandmeyer, Jamestown Community

College Pronde Sentistoven, Selt Leke Community

Brenda Santistevan, Salt Lake Community College

Linda Schmidt, Greenville Technical College

Ingrid Scott, Montgomery College

A.K. Shamma, University of West Florida Zachery Sharon, University of Texas at San Antonio

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Quizzes & Tests

Chapter Contents

Student Solutions

Online Review: Getting Ready for Precalculus

Study Plan

Gradebook

Chapter P

▼ Chapter 1

Getting Ready

Section 1.1

Section 1.2

Section 1.3

Section 1.4

Section 1.5

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•	*	More Objectives to practice and master			View all chapters	
	GR.1	Real Number System				
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	*	Find absolute values.	Practice	Quiz Me	0 of 1 MP	
	*	Calculate with real numbers.	Practice	Quiz Me	0 of 1 MP	
	*	Use the properties of real numbers.	Practice	Quiz Me	0 of 1 MP	
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Chapter P Mid-Chapter Check Point H

The Study Plan makes studying more efficient and effective for every student. Performance and activity are assessed continually in real time. The data and analytics are used to provide personalized contentreinforcing concepts that target each student's strengths and weaknesses.

Getting Ready \circ

Students refresh prerequisite topics through assignable skill review quizzes and personalized homework integrated in MyMathLab.

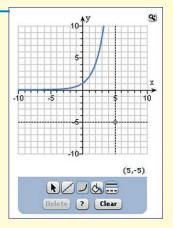
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– Video Assessment

Video assessment is tied to key Author in Action videos to check students' conceptual understanding of important math concepts.

Enhanced Graphing Functionality \circ -

New functionality within the graphing utility allows graphing of 3-point quadratic functions, 4-point cubic graphs, and transformations in exercises.



Skills for Success Modules are integrated within the MyMathLab course to help students succeed in collegiate courses and prepare for future professions.

Retain Your Knowledge These new exercises support ongoing review at the course level and help students maintain essential skills.

Instructor Resources

Additional resources can be downloaded from **www.pearsonglobaleditions.com/sullivan**.

TestGen®

TestGen[®] (www.pearsoned.com/testgen) enables instructors to build, edit, print, and administer tests using a computerized bank of questions developed to cover all the objectives of the text.

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Fully editable slides correlated with the text.

Instructor Solutions Manual

Includes fully worked solutions to all exercises in the text.

Mini Lecture Notes

Includes additional examples and helpful teaching tips, by section.

Online Chapter Projects

Additional projects that give students an opportunity to apply what they learned in the chapter.

Student Resources

Additional resources to enhance student success:

Lecture Video

Author in Action videos are actual classroom lectures with fully worked out examples presented by Michael Sullivan. All video is assignable within MyMathLab.

Chapter Test Prep Videos

Students can watch instructors work through step-by-step solutions to all chapter test exercises from the text. These are available in MyMathLab and on YouTube.

uTube.



Guided Lecture Notes

These lecture notes assist students in taking thorough, organized, and understandable notes while watching Author in Action videos. Students actively participate in learning the how/why of important concepts through explorations and activities. The Guided Lecture Notes are available as PDF's and customizable Word files in MyMathLab. They can also be packaged with the text and the MyMathLab access code.

Algebra Review

Four chapters of Intermediate Algebra review. Perfect for a slower-paced course or for individual review.



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